ORIE 5355

Project description, game theory/competition

Nikhil Garg

Plan for rest of the semester

Almost there!

Rest of semester

- Class project
- Miscellaneous lectures, guest lectures
 - Quiz 5
 - Attendance

Project Overview

Deadlines

Official deadlines

- Part 1 November 21
- Part 2 December 3 [BUT DO NOT WAIT TO START]
- Report December 12

Can submit edits to Part 1 + Part 2 at report deadline if absolutely needed (substantial points deduction)

Earlier "deadlines"

Starting this week, will start running preliminary Part 1 tournaments

• Such earlier submissions highly recommended for debugging purposes!

Will also start running preliminary Part 2 tournaments soon

Part 1 overview

- You and a single competitor (your classmates) each are selling one identical item, Book A.
- A customer walks in and you magically see their valuation for item v
- You and your competitor post prices for each item
- The customer buys from one of you, or neither
 - If minimum price < v, buys from minimum price seller
- Repeat for many more customers
- Objective: maximize revenue across games (1 game against each team)

Deliverable: Code for competitive pricing

Part 2 overview

Changes from Part 1:

- Now are selling 2 items, Book A and Book B.
- Observe customer covariates
- => Even without competition, must do demand estimation + price optimization

Deliverables

- Non-competitive demand estimation + price optimization:
 - For a set of test customers, what prices would you set for each customer for each item to maximize revenue, if you didn't have to worry about competition?
- Code for competitive pricing

Grading

| Project report | 0-6 points | How clearly + well did you <i>discuss</i> your strategy and evaluation techniques? How thoughtful was your reflection? |
|--------------------|------------|---|
| Project Part 1 | 0-6 points | How thoughtful and effective was your strategy? Does it reflect substantial effort? This will be influenced by objective performance, description in your report, and looking at your code. |
| Project Part 2 | 0-6 points | Same as Part 1 above |
| Overall subjective | 0-2 points | |

For grades: performance matters, but strategy/analysis matters more

Code Submission information

- Via GitHub classroom!
- Github classroom has an autograder that checks file structure and packages!

Summary

- Fill out the google form with your team's information. At least 1 team member needs GitHub username
- Have 1 team member click on github classroom invite link and "create" the team (use same team name as form)
 - This creates a repository
 - Everyone else can click on same link and join the team via team name.
- Rename "yourteamname.py" agent file
 - And rename "yourteamname/" folder. Allowed to put data/pickled machine learning models/etc into this folder
- Submission of code is just via pushing to the repository

How to avoid common submission mistakes

- Do **not** edit files other "yourteamname.py" or "yourteamname/" (or at least, do not rely on those edits for your code to work)
- Do not edit function names inside "yourteamname.py" file
- Yes: Edit above file names "yourteamname.py", "yourteamname/" with your team name
- Only put your required data or machine learning models in the folder "yourteamname/" inside the agents folder
- Yes: Use *relative* paths when loading data in your agent

```
CORRECT: filename = 'agents/yourteamname/trained_model'
```

NOT CORRECT: filename =

'c:/Users/Nikhil/documents/ORIE5355bestclassever/project/agents/
yourteamname/trained_model'

Part 1 suggestions + brief intro to game theory

More broadly: game theory, pricing competition

Challenge with competition

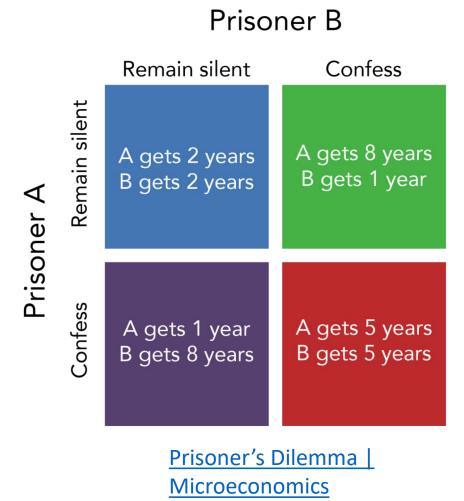
- There's now a game theory component: you need to anticipate what your opponent will do when setting prices
- You and your opponent both do the same thing, and calculate the exact same price p at the current time step
- Your opponent is clever, and so decides to *undercut* you slightly, and so sets price p-\$0.01
- ...but you're cleverer, and know your opponent will do this, and so you set prices p-\$0.02
- ... You keep doing this, and you're both setting prices p=0
- You can't ignore your opponent, otherwise they'll undercut you and always win the customer

Aside: game theory

Game theory: "study of mathematical models of strategic interactions among rational agents"

Example: Prisoner's dilemma

- 2 players
- Each can take 1 of 2 actions
- Have to choose action without knowing what other person chose
- No matter what other person does, you're better off confessing



(lumenlearning.com)

What about *repeated* games?

- In many settings, you're playing a *repeated* game
- Sometimes, repeated games change optimal behavior:
 - If I betray you today, you can retaliate by betraying me tomorrow
 - If I remain cooperate today, you can reward me tomorrow
- ...but, calculating optimal strategies in repeated settings can get complicated
- There are tournaments where people just play repeated prisoner's dilemma against each other. Person with most utility overall wins
 - "tit-for-tat" is often a top performing strategy

Pricing in repeated settings

- By the logic of a previous slide, setting prices p=0 is only rational response if you want to win the customer
- BUT, your objective isn't to win the customer, it's to make the most money overall. (and you know your opponent's goal is the same)
- What you do should depend on your opponent's actions
 - If they tend to price low, you should also price low
 - If they tend to price high, you should also price high
- But your actions affect your opponent's future actions!
 How do you avoid a price war?

Part 2: 2 items, user covariates

Step 1: Demand estimation + price optimization (HW 3...again)

Demand estimation

- Given buyer covariates and (single seller) prices p_A , p_B : what is the probability that the buyer buys item A? Item B? neither item?
- Task: train a machine learning model given the training data
 - (Data is now in the repository)

Price optimization

- Given your demand estimation, what are optimal prices p_A , p_B ? (to maximize revenue if you didn't have competition?)
- Now, have to do "2-dimensional" optimization.

Deliverable: optimal non-competitive prices for a set of customers

Step 2: Competition

Put Project Part 1 together with demand estimation/price optimization:

How to adjust your estimated prices over time against each opponent?

Questions?